

ME 322: Advanced Solid Mechanics (3-0-0:3)

Introduction

Review of basic concepts and equations in mechanics, Classification of materials, Outline of general techniques to solve boundary value problems

Mathematical Preliminaries

Indexical notation, Introduction to tensors, Representation of tensors, Gradient and related operators, Divergence theorem

Kinematics

Motion field, Displacement field, Deformation gradient, Transformation of curves, surfaces and volumes, strain measures, linearized strain measures, Principal strains and principal directions, Transformation of strain components with changes in coordinate basis, Compatibility conditions for linearized strain

Traction and Stresses

Concept of traction, Cauchy's stress theorem, Postulate of Cauchy stress tensor, Traction on arbitrary planes, Extreme normal and shear traction, Octahedral shear stress, Other stress measure - Engineering stress

Equilibrium Equations

Derive equilibrium equations in Cartesian and cylindrical polar coordinates

Constitutive Relations

Restrictions on constitutive relations, General relationship between Cauchy stress and Cauchy Green strain for isotropic materials, General Hooke's law and its reduction for isotropic and orthotropic materials

Boundary Value Problems

Displacement method, Stress method, Airy's stress functions for plane stress and strain problems, Uniaxial Tension, Thick-walled annular cylinder subjected to uniform boundary pressure, Infinite medium with a stress-free hole under far field tension loading

Bending of Prismatic Straight Beams

Pure bending, bending due to uniform transverse loading and bending due to transverse sinusoidal loading of a beam, Asymmetrical bending of straight beams, Shear center, Shear stresses in thin walled open sections

End Torsion of Prismatic Beams

Formulation of the BVP for torsion of beams with solid cross section - warping function and Prandtl stress function approach, Torsion of circular, elliptic, rectangular and triangular cross sections, Membrane analogy, Torsion of thin walled tubes, thin rectangular sections, rolled sections and multiply connected sections

Bending of Curved Beams

Winkler-Bach Formula, Elasticity solution for: pure bending of curved beams, curved cantilever under end loading

Beam on Elastic Foundation:

Derivation of the basic governing equation, Solution to beam on an elastic foundation subjected to a point load at the center, moment at the center, uniformly distributed load over some length 'a' symmetrically about the center

Text Books:

1. L.S. Srinath, "Advanced Mechanics of Solids", Tata McGraw Hill
2. A.R. Ragab, and S.E. Bayoumi, "Engineering Solid Mechanics: Fundamentals and Applications", CRC Press

References:

1. M.H. Sadd, "Elasticity: Theory, Applications and Numerics", Academic Press

