

CS 416: Computational Geometry (3-0-0: 3)

Introduction

Historical perspective, geometric preliminaries.

Convex hulls

Convexity and convex hulls, naive algorithms for extreme points, Gift wrapping, Quick Hull, Graham's algorithm, incremental algorithm, divide and conquer, lower bounds.

Line segment intersection

Line segment intersections, plane-sweep, doubly-connected edge list, overlay subdivisions.

Polygon triangulation

Triangulating monotone polygons, partitioning simple polygons, convex partitioning, lower and upper bounds, linear time triangulation.

Linear programming

The geometry of casting, half-plane intersections, incremental and randomized algorithms, unbounded linear programs, linear programming in higher dimension.

Orthogonal search

Geometric data structures, 1-D range searching, quad-tree, kd-tree; improvements on range searching, range tree; fractional cascading, inverse range search - segment tree, interval tree; priority search tree.

Voronoi diagrams and Delaunay triangulations

Voronoi diagrams, furthest point Voronoi diagram, other distance metrics, Fortune's plane sweep algorithm, Delaunay triangulation- empty circles, local Delaunay-hood, randomized incremental algorithm, backward analysis.

Visibility

Algorithms for weak and strong visibility, visibility with reflections, art-gallery problems.

Point location

DAG structure for point location in triangulations, a randomized incremental algorithm, degenerate cases.

Arrangements

Duality, line arrangements, levels and discrepancy, complexity, incremental algorithm, zone theorem.

Applications of computational geometry.

Text Books:

1. M. de Berg, M. van Kreveld, M. Overmars, and O. Schwarzkopf, "Computational Geometry: Algorithms and Applications", Springer.
2. F. P. Preparata and M. I. Shamos, "Computational Geometry: An Introduction", Springer.

References:

1. J. O'Rourke, "Computational Geometry in C", Cambridge University press.
2. T. H. Cormen, C. E. Leiserson, R. L. Rivest, and C. Stein, "Introduction to Algorithms", MIT Press.
3. R. Motwani and P. Raghavan, "Randomized Algorithms", Cambridge University press.